

系所組：化學系應用化學碩士班

日期節次：101 年 3 月 17 日 第 3 節 13:00~14:30

科目：物理化學

1. (a) One mole of an ideal gas at 300 K is reversibly and isothermally compressed from 25.0 L to 10.0 L. Suppose the surrounding is also at 300 K, calculate  $\Delta S$  and  $\Delta S_{\text{surrounding}}$ . (10 points)  
(b) Under the same condition of Problem 1(a) except the compression is now done by a constant external pressure  $2.49 \times 10^5$  Pa, is the process spontaneous or non-spontaneous? Why? (10 points)
2. A prolate molecule like  $\text{CH}_3\text{I}$  has moment of inertia  $I_a < I_b = I_c$ , show that its rotational energy can be expressed by  $E_{JK}(\text{cm}^{-1}) = BJ(J+1) + K^2(A-B)$ , where J and K are quantum numbers, A and B are rotational constants. (10 points)
3. Draw the  $\pi$  orbitals of benzene and fill in the  $\pi$  electrons. (10 points)
4. Derive the equilibrium constant of reaction  $\text{CaCO}_{3(s)} \rightleftharpoons \text{CaO}_{(s)} + \text{CO}_{2(g)}$  in terms of substance activities. (10 points)
5. Suppose an enzyme catalyzed reaction has mechanism  $\text{E} + \text{S} \xrightarrow{k_1} \text{ES}, \text{ES} \xrightarrow{k_{-1}} \text{E} + \text{S}, \text{ES} \xrightarrow{k_2} \text{E} + \text{P}$ . Here E, S, ES and P stand for the enzyme, substrate, intermediate, and product, respectively. If the initial concentration of E is  $[\text{E}]_0$ , derive the rate law by the steady-state approximation. (10 points)
6. (a)  $\text{SO}_2$  is a  $\text{C}_{2v}$  molecule and the  $p_x$  orbitals are defined as perpendicular to this exam paper. Now with the  $p_x$  orbitals of S,  $\text{O}_A$ , and  $\text{O}_B$  atoms as the basis ( $p_S, p_A, p_B$ ), derive the matrix representation of the  $\text{C}_2$  axis with respect to this basis. (10 points)  
(b) If we have a new basis ( $p_S, p_1, p_2$ ), where  $p_1 = p_A + p_B$  and  $p_2 = p_A - p_B$ , derive the matrix representation of the  $\text{C}_2$  axis with respect to this new basis. (10 points)
7. Term explanations: (5 points for each)
  - (a) The third law of thermodynamics.
  - (b) Arrhenius preexponential factor.
  - (c) The uncertainty principle.
  - (d) Normalized wave functions.